Traffic Engineering vs. Content Distribution

A Game-Theoretic Perspective

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Overview

- **Traffic Engineering** is the optimal assignment of **users** to **routes** in a network
- **Content Distribution** involves **users** selecting content from various **servers**
- These two may be in **conflict**!
 - The Traffic Engineer does not anticipate that users may change behavior in response to his decisions!

The Traffic Engineer

- Sees current traffic between **users** and **servers**
- Assigns **routes** to each **user-server** pair
 - Routes may involve overlapping resources (e.g. links)
 - Flows through **resources** generate **congestion**
- Given traffic $ec{e}$ the engineer chooses a routing policy $ec{\pi}$
 - He wants to minimize the total congestion at the resources:

• Flows:
$$f_j(\vec{e}, \vec{\pi}) = \sum_{ms} \sum_{r: j \in r, r \in R_{ms}} \pi_{mrs} e_{ms}$$

The Traffic Engineer

Route 1 Server 1 0 Route 2 Server 2 0 Route 3 The User Server 3 0 Splits determined by routing policy Total traffic for Server 3

Total traffic for Server 1

The Users

- See current **routing assignment**
- Choose how much traffic to request from each **server**
- Given routing policy $\vec{\pi}$ the users select servers and generate traffic \vec{e}
 - They want to minimize the **price** they pay to access servers



Prices and Latency

- Users of distributed content often use **signals** when choosing servers
- Example of a signal: **delay** or **latency** to the server
- Abstraction: flow-dependent **price** $p_j(f_j)$ on each link j
 - Price may simply be the **delay** $l_j(f_j)$ of link j
 - Or some more complicated function:

 $p_j(f_j) = l_j(f_j) + f_j l'_j(f_j)$

- Price of a **route** is the sum of prices of its links
- Price to a **server** is the average price of its routes, as determined by the Traffic Engineer's **routing policy**

Prices and Wardrop Equilibria

- We assume users are **infinitesimal**
 - Individually, their decisions do not greatly impact the flows
- Collectively, in **equilibrium**, they only communicate with servers that have the minimum prices
- The resulting traffic implicitly minimizes an **objective** function: $\sum_{j} \int_{0}^{f_{j}} p_{j}(t) dt$
 - This is the **implicit objective function** of the users

The Importance of Optimism

Zero traffic for Server 1



Pigovian Taxes

- Suppose the **delay** on a link is $l_j(f_j)$
- Then the **total delay** on that link is $f_j l_j(f_j)$
- Problem: Users do not account for the delay they impose on others through their decision!
- Solution: Charge them a **Pigovian tax**
 - Have them act as if delay (price) is $l_j(f_j) + f_j l'_j(f_j)$
 - The extra term forces them to **internalize** the effect they have on others

Unified Objectives

- When the Traffic Engineer's congestion function is total delay: L_j(f_j) = f_jl_j(f_j)
- And the Users' price function has a **Pigovian tax**:

$$p_j(f_j) = l_j(f_j) + f_j l'_j(f_j)$$

- Then both parties have the **same objective function**
- There is **only one equilibrium**, and it is the **best possible outcome** (i.e. total delay is minimized over all server choices and routing policies)

Dynamics

- Traffic Engineering is typically done on a **slow timescale**, e.g. a few times a day
- Users of distributed content may change their servers very quickly
 - So between changes by the Traffic Engineer, the users have time to converge to the **Wardrop Equilibrium**
- Under Unified Objectives, these dynamics converge to the best possible outcome
- With different objectives, the dynamics may be unstable and suboptimal

Extensions

- The results extend gracefully to:
 - Multiple classes of users
 - Multiple types of content
 - General overlay networks
 - Delays at the servers
- With some additional assumptions, we can also extend to:
 - Multiple ISPs (and multiple Traffic Engineers)
 - Requires that users are the ones who control inter-domain routing

Conclusion

- Traffic Engineering and Content Distribution may result in **conflicting** and **unanticipated** decisions by the relevant parties
- With the use of **Pigovian taxes**, the objectives of the users and the Traffic Engineer may be aligned
 - When objectives are aligned, the equilibrium outcome is **predictable** and **optimal**
- These considerations may aid in the design of content distribution systems

Related Work

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