# COMPUTER FORUM 09

Modeling Structural Heterogeneity in Proteins From X-Ray Crystallography Data

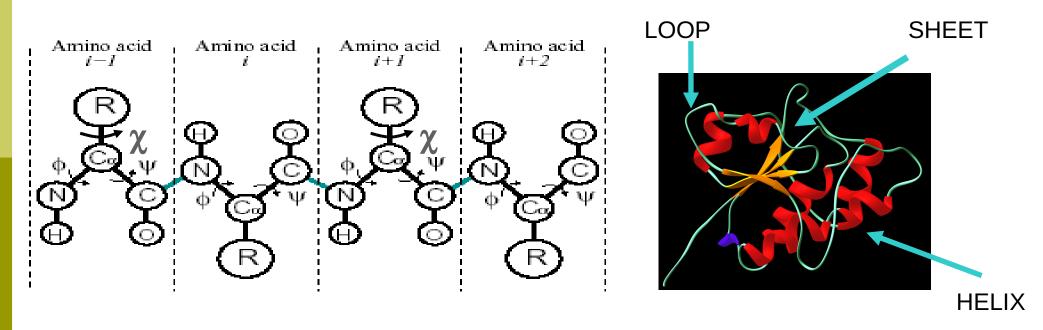
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## Protein

# Sequence of amino acids (residues) connected with peptide bonds

- Forms kinematic chain with many DOFs
- Folds spontaneously into a compact structure



## Protein

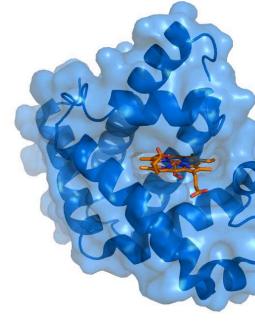
Proteins are building blocks of human body

Calcium binding protein

- The function of a protein depends on its folded structure
- Protein-ligand binding requires geometric/chemical complimentarity

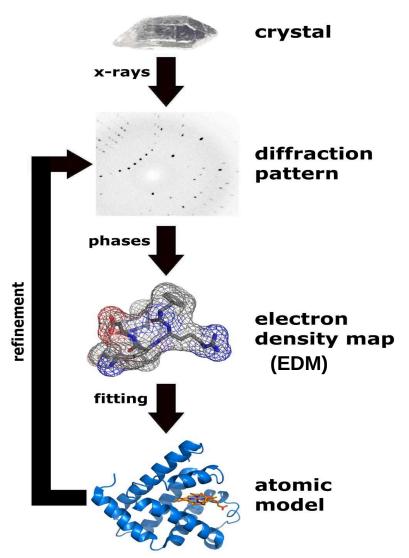
→ Correctly determining protein's structure is critically

important



# X-Ray Crystallography

- Main experimental technique for determining protein structures
- About 90% structures deposited in Protein Data Bank have been determined using this technique



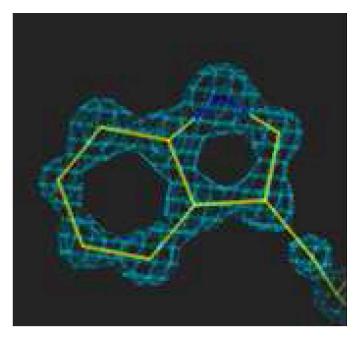
# Joint Center for Structural Genomics

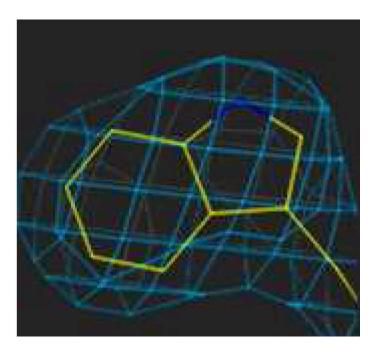
- Part of Protein Structure Initiative
- One of four large-scale protein structure determination centers funded by NIH
- As of now 747 structures deposited in PDB (Protein Data Bank)



# X-Ray Crystallography Challenges

- Low data resolution
- Data collection noise, impurities



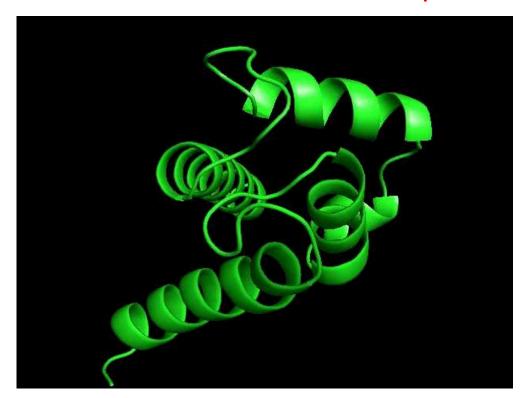


1.0Å

3.0Å

# X-Ray Crystallography Challenges

- Structural heterogeneity
  - High-frequency thermal vibration of atoms
  - Low-frequency diffusive motions (coordinated motions of multiple atoms)
  - Diffusive motions are critical to the protein's function

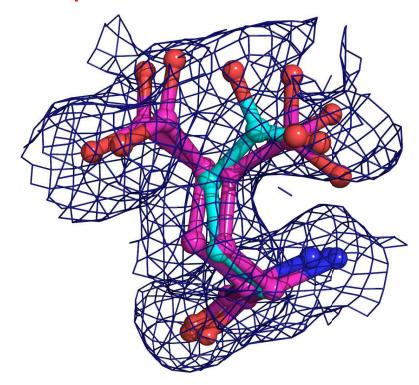


# X-Ray Crystallography Challenges

- Structural heterogeneity
  - High-frequency thermal vibration of atoms
  - Low-frequency diffusive motions (coordinated motions of multiple atoms)
  - Diffusive motions are critical to the protein's function

→ Multiple conformations are present in a crystal

Diffraction pattern is occupancy weighted superposition of patterns (*Occupancy*: percentage of copies of a conformation)



# X-Ray Data Modeling

#### Current practice

- Compute one "average" protein conformation
- Explain thermal vibrations with isotropic Gaussian distribution of atom position controlled by temperature factor or B-factor
- Software suites: ARP/ RESOLVE/ TEXTAL

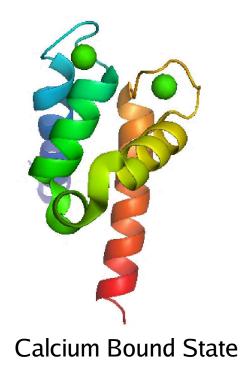
#### But: Is one solution enough?

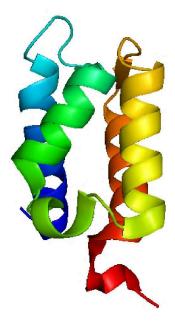
- Several "average" conformations can explain the EDM equally well (Terwilliger, 2007)
- Modelling structural heterogeneity is critically important (Furnham 2006, DePristo 2004)

# Modeling Heterogeneity

#### Our goal

- Compute an ensemble of conformations (with occupancies and B-factors) that, collectively, provides a near-optimal explanation of the EDM
- Current focus: fragments with deformable kinematics (mainly loops and side chains)

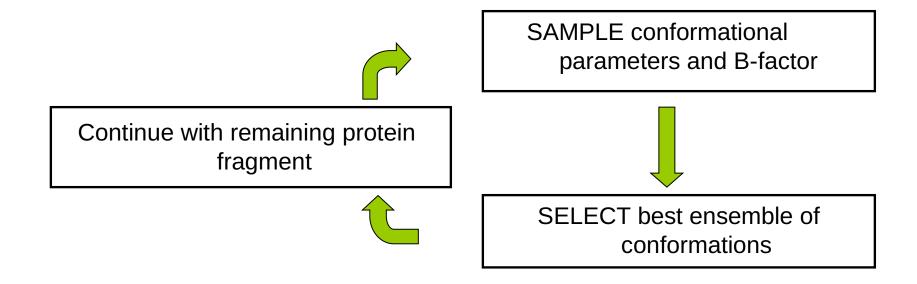




# Modeling Heterogeneity

#### Our Method

Alternate SAMPLE (massive sampling) and SELECT (efficient selection) steps



# Modeling Heterogeneity

#### **SELECT**

Uses linear programming to compute occupancies and select conformations with non-zero occupancies

Find  $\alpha_1, ..., \alpha_N$  such that

 $\sum_{p \in G} | E(p) - \sum_{i} \alpha_{i} E_{i}(p) |$  is minimum,

Under the constraints:

 $\alpha_i \ge 0$  for all i=1, ..., N and  $\sum_i \alpha_i = 1$ 

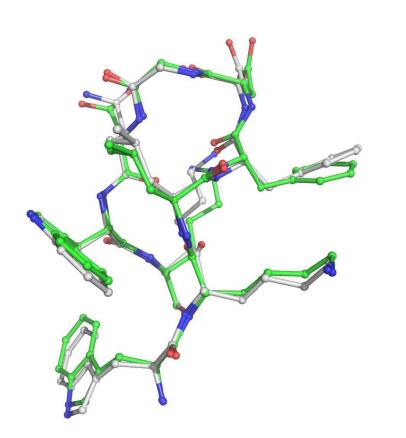
 $\alpha_i$  = occupancy of conformation i

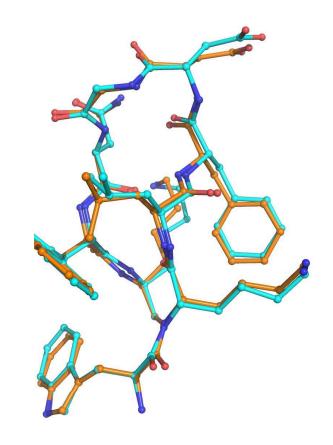
E(p) = electron density of given EDM at grid point p

 $E_i(p)$  = electron density of EDM computed from conformation i at grid point p

- Simulated and experimental EDMs
- Simulated EDMs are computed over a range of resolution levels, noise levels, occupancies, and B-factors
- Reasonably accurate conformations, occupancies, and B-factors are computed
- Libraries used: LoopTK, Clipper, Coin-OR

- 2R4I (loop 104-112)
  - Two conformations, separated by 1.4 Å RMSD (root mean squared distance between corresponding atoms)
  - Average B-factor =  $19.0 \text{ Å}^2$
  - Simulated EDM is generated at different resolutions and occupancies
  - Gaussian noise is added





Осс	Res	RMSD	Calc Occ	Bcalc
0.7/0.3	1.3	0.27 0.34 0.34 0.34 0.64	0.70	24.1
		0.48	0.30	

### □ 1HFC (loop 142-149)

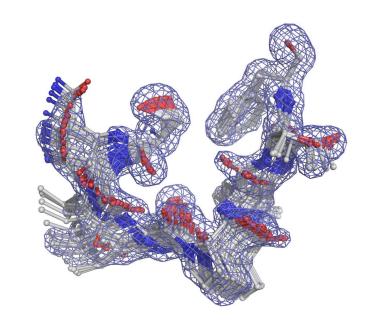
- 20 conformations
- Emulates coordinated motion of the loop
- Start and finish conformations 2.7Å RMSD apart
- Average B-factor = 11.7 Å<sup>2</sup>
- Simulated EDM is generated at equal occupancy (0.05) and 1.9 Å resolution

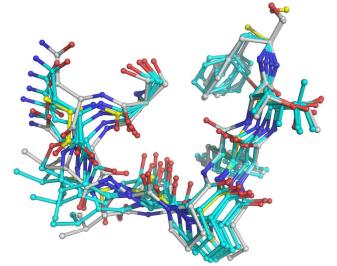
#### Our method

- 7 conformations, occupancies ranging from 0.10 to 0.23
- Average B-factor =  $15.0 \text{ Å}^2$

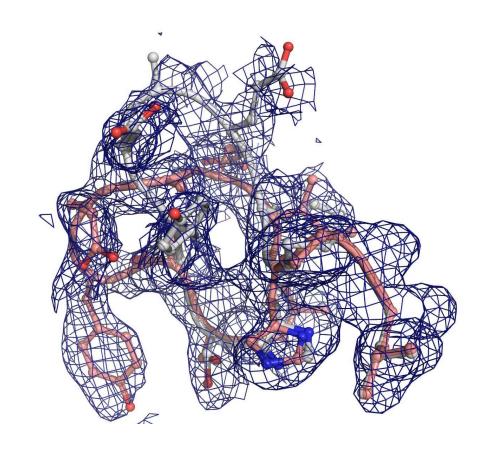
#### RESOLVE

- 1 conformation
- Average B-factor =  $35.7 \text{ Å}^2$

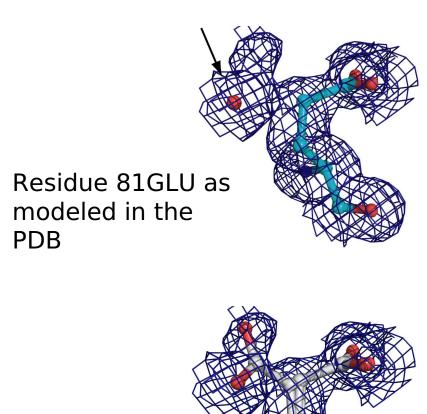


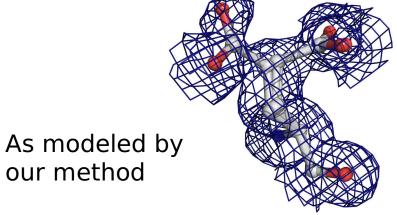


- TM0755 (loop 316-325)
  - Experimental data from JCSG at 1.8 Å resolution
  - Difficult to model (even for trained crystallographers)
  - Two conformations
  - Average JCSG B-factor = 24.9 Å<sup>2</sup>
  - 5 conformations computed
  - 0.47(0.15), 0.64(0.27)
  - Average B-factor =  $30.3 \text{ Å}^2$



- 2NLV (multiple side chain conformations)
  - Experimental data from JCSG at 1.3 Å resolution
  - PDB conformation contains water molecule in place of carbonyl oxygen
  - Our method modeled 12 multi-conformation alternatives for single conformation residues with improved fit to EDM

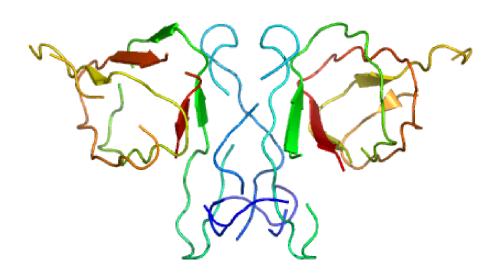




# Is one solution enough?

#### NO!

JCSG has deposited two new structures in PDB using our method, including the highly heterogeneous protein 3EO6



# Is one solution enough?

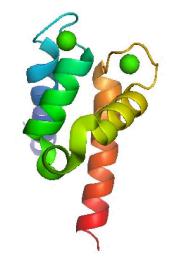
#### □ NOi

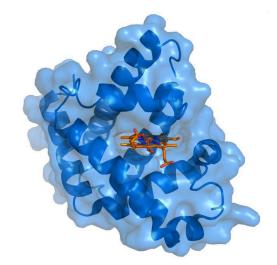
JCSG has deposited two new structures in PDB using our method, including the highly heterogeneous protein 3EO6

 Our method demonstrates that heterogeneity in EDM can be better explained by multiple conformations than by B-factors alone

## Protein revisited

- Proteins are building blocks of human body
- The function of a protein depends on its folded structure
- Protein-ligand binding requires geometric/chemical complimentarity
- → Correctly determining protein's structure is critically important





Our method can lead to better determination and understanding of protein's structure, and provide insights into its functioning

# Acknowledgements

- NSF award DMS-0443939, CNS0619926
- JCSG